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Cryogenic reconfigurable logic with superconducting heater cryotron: Enhancing area efficiency and enabling camouflaged processors ✓

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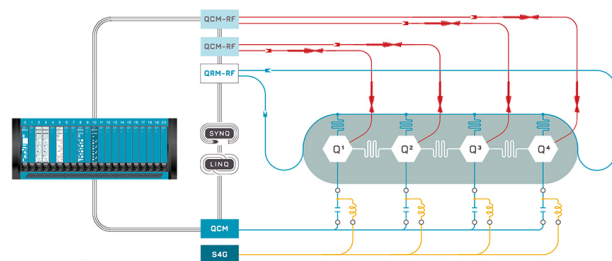
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ABSTRACT

Superconducting electronics are among the most promising alternatives to conventional CMOS technology, thanks to the ultra-fast speed and ultra-high energy efficiency of the superconducting devices. Having a cryogenic control processor is also a crucial requirement for scaling the existing quantum computers up to thousands of qubits. Despite showing outstanding speed and energy efficiency, Josephson junction-based circuits suffer from several challenges such as flux trapping leading to limited scalability, difficulty in driving high impedances, and so on. Three-terminal cryotron devices have been proposed to solve these issues, which can drive high impedances ($> 100 \text{ k}\Omega$) and are free from any flux trapping issue. In this work, we develop a reconfigurable logic circuit using a heater cryotron (hTron). In conventional approaches, the number of devices to perform a logic operation typically increases with the number of inputs. However, here, we demonstrate a single hTron device-based logic circuit that can be reconfigured to perform 1-input copy and NOT, 2-input AND and OR, and 3-input majority logic operations by choosing suitable biasing conditions. Consequently, we can perform any processing task with a much smaller number of devices. Also, since we can perform different logic operations with the same circuit (same layout), we can develop a camouflaged system where all the logic gates will have the same layout. Therefore, this proposed circuit will ensure enhanced hardware security against reverse engineering attacks.

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Superconducting processors have garnered renewed interest in the past few decades primarily due to their promise as controllers for qubit programming/readout in large-scale quantum computing systems.^{1–5} In addition, they are uniquely suited for exa-scale high-performance computing systems and space applications.^{6,7} Josephson junction (JJ)-based logic families are the primary building blocks of superconducting Boolean logic. Thanks to the ultra-fast ($> 100 \text{ GHz}$) and ultra-low power (sub-aJ/bit switching energy) operation of JJ-based circuits,^{8,9} a superconducting processor has the potential to solve many existing issues of its CMOS counterpart. However, JJ-based circuits suffer from a number of challenges, including difficulty in cascading, fabrication challenges, limited scalability due to flux trapping and sensitivity to magnetic field, and so on.^{10,11} To solve some of these challenges, three-terminal cryotron devices were developed, which show input gate current-driven switching of the channel between its superconducting and resistive states.¹⁰ The heater cryotron (hTron)¹²

is a member of this cryotron family. These devices can drive large impedances ($> 100 \text{ k}\Omega$) and support a large number of fanouts due to their transition to a highly resistive state. Moreover, these devices do not require superconducting loops like JJs and, hence, are free from flux trapping and resulting scalability issues.¹⁰ hTron devices have already been used as an access device in cryogenic memories,^{13–15} as an interface between superconductors and semiconductors,¹² to design logic circuits,^{10,11,16,17} in cryogenic neuromorphic systems,^{18–21} and so on.

Despite being used in several sensitive and critical applications, the hardware security techniques for superconducting processors are yet to be developed. Therefore, the superconducting processors are alarmingly vulnerable to different adversarial attacks, including integrated circuit (IC) counterfeiting, IC masking, IC overproduction, intellectual property (IP) piracy, reverse engineering, etc. To prevent these attacks, different hardware security measures, including IC

camouflaging, logic locking, and/or adding a watermark, among others, are used. Among these, logic locking²² and IC camouflaging²³ have recently been utilized for developing secured superconducting hardware. In the logic locking technique, additional gates (AND, OR, XOR, etc.), key inputs, and additional on-chip memory are introduced into the original design to prevent external attacks. However, as reported in Ref. 22, the logic locking technique requires an additional 20% area overhead for only one OR gate. On the other hand, in IC camouflaging technique in Ref. 23, dummy JJs are introduced to make the layouts of all the gates look identical to prevent reverse engineering and other attacks. Both of these techniques have a significant negative impact on the area, delay, and power consumption of the circuit.

In this work, we demonstrate a superconducting reconfigurable logic circuit with a single hTron device that can perform the basic Boolean logic operations, including 1-input copy and NOT, 2-input AND and OR, and 3-input majority. Typically, the number of devices required to perform any logic operation increases with the number of inputs.^{10,11} However, in our proposed circuit, we perform all the above-mentioned single- and multi-input logic operations with only one hTron device. We apply different biasing conditions in the same circuit to perform all these logic operations. Thanks to the reconfigurability of the proposed circuit, it requires significantly less area compared to the existing superconducting logic circuits based on JJs, SQUIDs, and cryotrons. Moreover, as we are using the same circuit with the same layout to perform different tasks, we can build a camouflaged system (without compromising on any performance metric), where all the logic gates will look identical which can improve the hardware security of the system.

We start our discussion with the device characteristics of an hTron. hTron is a four-terminal current-driven superconducting device where two of the terminals form the gate and the other two form the superconducting channel [Figs. 1(a)–1(c)]. The gate and channel microwires are separated by a 25 nm SiO₂ dielectric spacer. The dielectric spacer electrically isolates but thermally couples the two microwires. Details on the device fabrication are available in the supplementary material.

Initially, the channel remains superconducting for a given channel bias current (I_{Ch}) and no gate current (I_G). However, when I_G is applied, the gate becomes resistive and generates thermal phonons, which are carried to the channel by the dielectric spacer. The channel remains superconducting until I_G exceeds a specific threshold and becomes resistive [Fig. 1(b)]. However, when the gate becomes resistive, the presence of these thermal phonons suppresses superconductivity in the channel, and the more gate current is added, the greater the suppression of I_{Ch}^C is observed [as shown in Fig. 1(d)]. The reason for suppressing the superconductivity is that the thermally generated phonons are capable of breaking Cooper pairs in the superconducting channel [Fig. 1(c)]. When I_G exceeds a specific threshold (I_G^C) such that the channel critical current (I_{Ch}^C) [a function of I_G , shown in Fig. 1(d)] becomes smaller than the applied I_{Ch} , enough phonons with sufficient energy ($> 2\Delta$, where Δ is the superconducting energy gap²⁴) are generated, which can break Cooper pairs in the channel and cause the entire channel to switch to the high impedance resistive state, driving I_{Ch} to the external circuitry [Fig. 1(c)].

While characterizing the device, we first apply a fixed current to the gate (I_G). Then, we ramp up the channel bias current (I_{Ch}) from 0 A to above I_{Ch}^C , so that the channel switches. For each I_G , we perform

the ramping of I_{Ch} 50 times and record the I_{Ch}^C for each measurement. Figure 1(d) shows the measured distribution of I_{Ch}^C for I_G ranging from 10 to 135 μ A. We also extract the median of I_{Ch}^C for each I_G [Fig. 1(e)] and use that as the nominal I_{Ch}^C in our circuit design. Next, we perform a transient measurement to show the time dynamics of the channel switching from its superconducting to non-superconducting state. The inset of Fig. 1(f) shows the transient measurement setup with a load resistance of 1 k Ω . Here, we first ramp I_{Ch} up to 55 μ A and then start ramping up I_G to capture the gate-driven switching [Fig. 1(f)]. As shown in Fig. 1(g), initially, the channel is in its superconducting state, and, hence, no current flows through the load resistor ($I_L = V_L \approx 0$). However, when I_G exceeds I_G^C (110 μ A for this case), the channel switches to its non-superconducting state and drives I_{Ch} to the load resistor, which creates a nonzero voltage across it. The turn-on and turn-off times for the hTron device considered in this work are 300 ps and 15 ns, respectively. However, the turn-on and turn-off time can be reduced by using higher input energy and different superconducting material, respectively.¹² The WSi film used as the superconducting material had a critical temperature (T_C) of 3.5 K, and all the measurements were performed at 0.9 K. To obtain a higher operating temperature, a different material such as NbN or NbTiN can be used, which shows a T_C of 9–12 K depending on the stoichiometry. More details on the device characterization are available in the supplementary material.

In this work, we utilize the gate current-controlled superconducting to non-superconducting transition of the hTron to design a reconfigurable logic circuit for achieving secured superconducting hardware. We use the same measurement setup [shown in the inset of Fig. 1(f)] and measured device characteristics [Fig. 1(e)] to design the logic circuit. The only difference is that instead of one input current to the gate, we use three input currents to perform up to three-input logic operations. Figure 2(a) shows the schematic of the designed reconfigurable logic circuit, where I_{IN1} , I_{IN2} , and I_{IN3} are the input currents corresponding to the number of inputs of the logic operations, I_{B1} is a common gate bias used for all the operations, and I_{B2} is the channel bias. In our design, we define the two logic states (“0” and “1”) with two current levels (0 μ A and $I_G^C/2$, respectively) [Fig. 2(b)]. Figure 2(c) shows the biasing scheme that we use to perform different logic functions with the same circuit shown in Fig. 2(a). For all the logic operations, I_{B2} is kept fixed at 55 μ A [chosen based on the measured device data shown in Figs. 1(d)–1(g)]. Now, to perform different logic functions such as 1-input copy and NOT, 2-input AND and OR, and 3-input majority, we only need to apply different bias currents to I_{B1} [range is shown in Fig. 2(c)]. The combination of the input currents and I_{B1} will determine the switching of the channel under the fixed I_{B2} bias, and accordingly, we will get zero or nonzero current at the output.

To demonstrate the functionality of different logic functions with our proposed circuit, we adopt a simulation-based approach. We first develop a lookup-table (LUT) based compact model for the hTron in Verilog-A and calibrate the model with the measured data shown in Figs. 1(d)–1(g). In each time step, the model takes applied gate and channel currents as input, and based on the value of the gate current, it reads the corresponding I_{Ch}^C from the LUT. Finally, the model compares the applied channel current with the I_{Ch}^C obtained from the LUT and determines whether the channel will switch or not. As already mentioned, our proposed circuit is similar to the measurement setup.

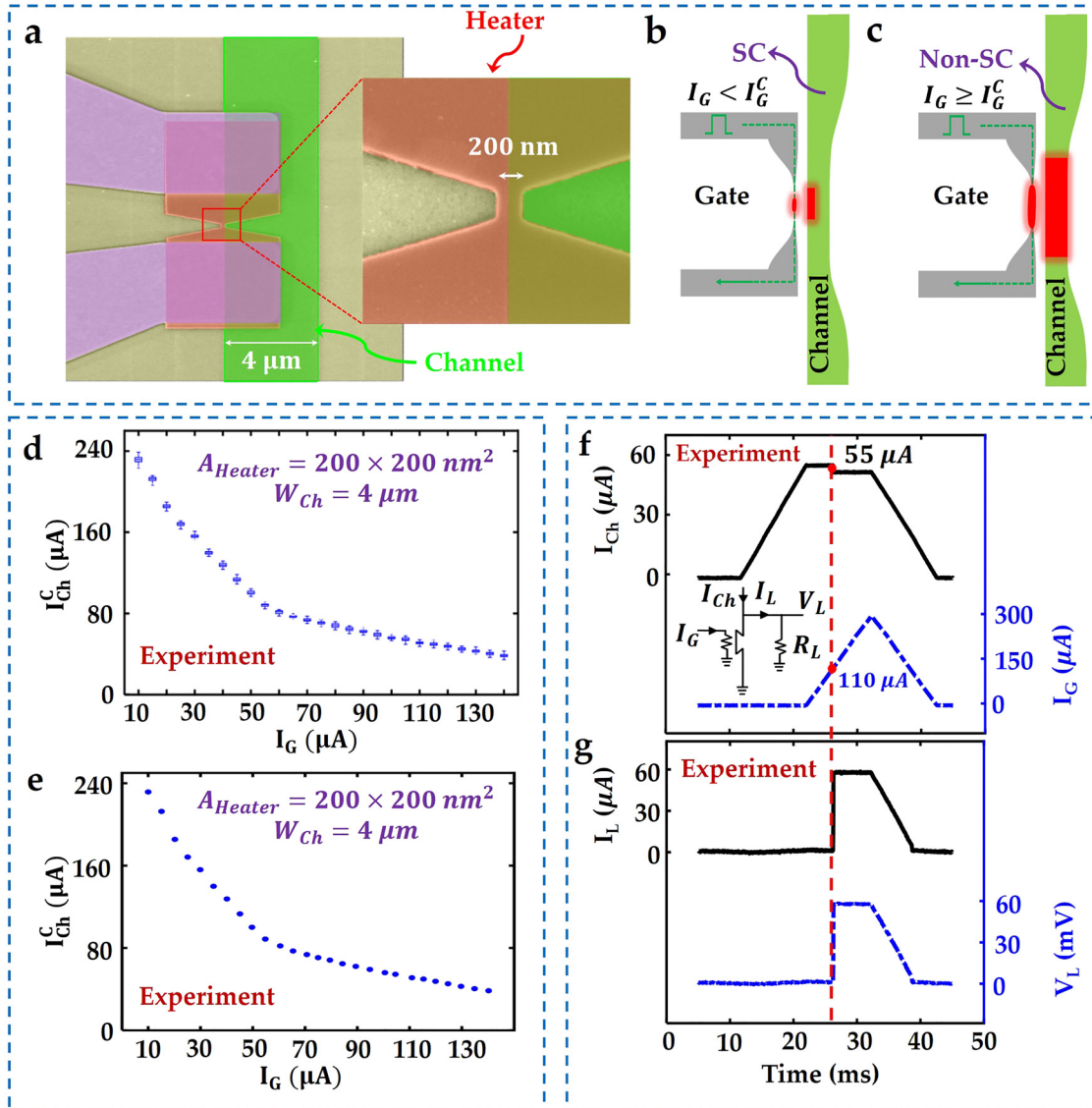


FIG. 1. Device characteristics of heater cryotron (hTron). (a) False-colored scanning electron micrograph (SEM) of a fabricated hTron device. The device consists of a resistive heater (gate) and a superconducting microwire (channel) separated by a SiO₂ dielectric spacer. The fabricated device has a heater gate with an area of $200 \times 200 \text{ nm}^2$ and a channel with a width of 4 μm . (b) and (c) Illustration of the switching mechanism of a the hTron device. (d) Measured distributions of the channel critical current (I_{Ch}^c) for different values of I_G (refer to FIG. S1 in the supplementary material for the zoomed-in views of the measured I_{Ch}^c distribution). (e) Extracted median values of I_{Ch}^c distributions for each I_G . (f) and (g) Measured time dynamics of the switching of a hTron device with a load resistance (R_L) of 1 kΩ .

The only difference is the use of multiple input currents applied to the gate. Note, all the input currents and I_{B1} are added together and seen as one bias current by the gate. Therefore, utilizing the experimentally calibrated device model, our simulation replicates the behavior that we would observe in the experiment.

First, we discuss the 1-input copy gate. Here, we use the $IN1$ terminal to apply the input current, and we apply 65 μA as I_{B1} and 55 μA as I_{B2} . As shown in Fig. 3(a), for a logic 0 at the input ($I_{IN1} = 0$), the total applied current to the gate is I_{B1} (65 μA), which is less than I_G^c

(110 μA), and hence, the channel remains superconducting. Therefore, I_{B2} flows through the channel, and we get logic 0 ($I_{OUT} = 0$) at the output. On the other hand, as shown in Fig. 3(b), when a logic 1 is applied ($I_{IN1} = I_G^c/2 = 55 \text{ μA}$), the total gate current ($I_G = 120 \text{ μA}$) exceeds I_G^c and switches the channel to its non-superconducting state, which is highly resistive. Therefore, I_{B2} flows through the external resistor ($R = 1 \text{ kΩ}$), and we get logic 1 ($I_{OUT} = I_G^c/2 = 55 \text{ μA}$) at the output. Figures 3(c)–3(e) show the simulated time dynamics of the copy gate, which verifies the functionality of the logic function.

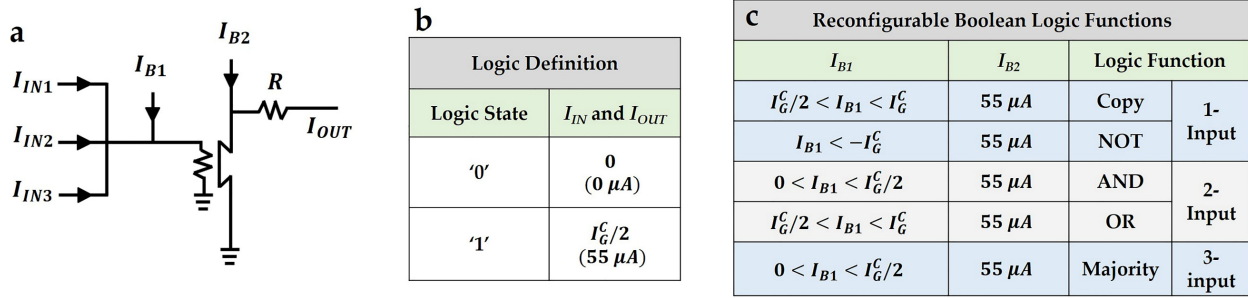


FIG. 2. Single hTron-based reconfigurable logic circuit. (a) Schematic of the hTron-based reconfigurable logic circuit that can perform 1-input copy and NOT, 2-input AND and OR, and 3-input majority operations with only a suitable bias current (I_{B1}). We use $1\text{ k}\Omega$ as the load resistor (R). (b) Definition of logic states. (c) Biasing conditions to perform different logic operations with the same circuit.

Next, we discuss the 1-input NOT gate where we use the same input terminal and same I_{B2} . The only difference is that we apply $-120\text{ }\mu\text{A}$ as I_{B1} . Now, when a logic 0 ($I_{IN1} = 0$) is applied, only I_{B1} flows through the gate, which itself is greater than I_G^C [Fig. 3(f)]. As a result, the channel of the device switches to the non-superconducting state and drives I_{B2} to the external resistor. Therefore, we get logic 1 ($I_{OUT} = I_G^C/2 = 55\text{ }\mu\text{A}$) at the output. However, when the input is logic 1 ($I_{IN1} = 55\text{ }\mu\text{A}$), the device gets a total gate current of $-65\text{ }\mu\text{A}$, which cannot switch the channel [Fig. 3(g)]. Hence, the channel remains superconducting, and we get 0 A at the output. Figures 3(h)–3(j) verify the NOT gate functionality.

With the same circuit, we can also perform 2-input Boolean logic functions such as AND and OR logic where we use two input terminals to apply the input currents (I_{IN1} and I_{IN2}).

To perform AND operation, we apply $I_{B1} = 10\text{ }\mu\text{A}$. As a result, for input combinations of 00 and 01 (or 10), the gate gets 10 and $65\text{ }\mu\text{A}$, respectively, which are not sufficient enough to switch the state of the hTron channel [Fig. 4(a)]. Therefore, the channel remains in its superconducting state and drives $0\text{ }\mu\text{A}$ (logic 0) to the output. On the

other hand, for the 11 input combination, a total current of $120\text{ }\mu\text{A}$ flows through the gate and switches the channel to the non-superconducting state [Fig. 4(b)]. Therefore, I_{B2} flows through the external resistor, and we get logic 1 ($55\text{ }\mu\text{A}$) at the output. The time dynamics of AND functionality are shown in Figs. 4(c)–4(e).

Next, to perform the OR operation, we apply $I_{B1} = 65\text{ }\mu\text{A}$. As a result, whenever one of the two inputs is logic 1, the gate terminal gets sufficient current to switch the channel of the device. Therefore, only for the input combination of 00, the channel remains superconducting, and for 01, 10, and 11 combinations, the channel switches to its non-superconducting state [Figs. 4(f) and 4(g)]. As seen in Figs. 4(h)–4(j), we get the OR operation.

Majority is a Boolean logic operation that generates an output of logic 1 if there are more number of logic 1 among an odd number of inputs. The majority logic can be utilized to perform the basic logic operations such as AND, OR, XOR, etc. and requires a lower number of gates to develop arithmetic-intensive systems.²⁵ Compared to the AND implementation, majority reduces the logical depth of the arithmetic-intensive circuits by up to 33%.²⁶ For example, while

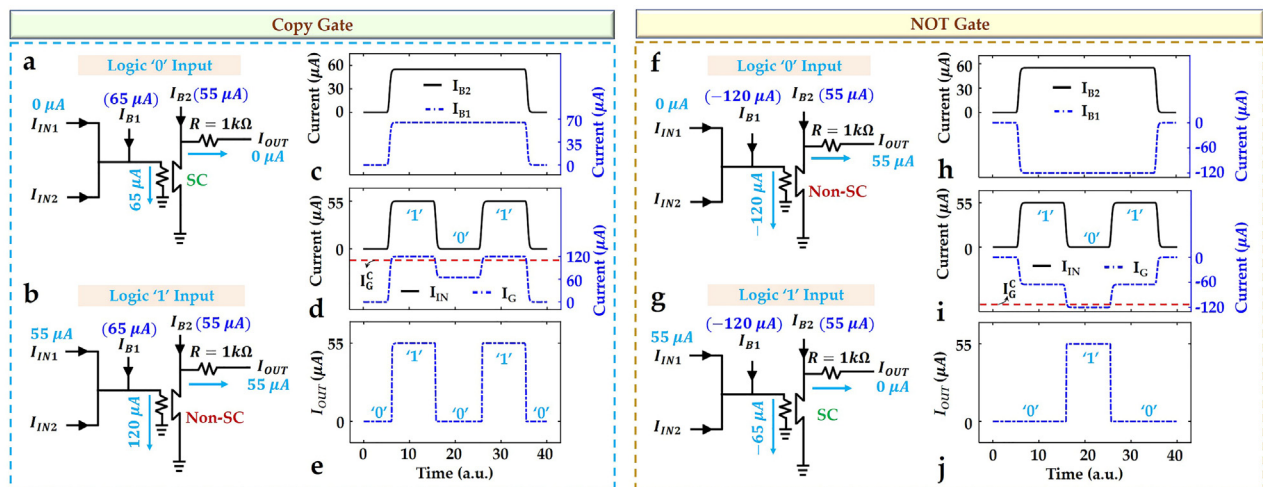


FIG. 3. 1-Input copy and NOT operations. Copy operation with the proposed circuit when the input is (a) logic 0 and (b) logic 1. (c)–(e) Simulated time dynamics of the copy operation. (f) and (g) Illustration of the NOT operation for logic 0 and 1 inputs, respectively. (h)–(j) Time dynamics of the NOT operation where the channel switches for logic 0 input due to the choice of I_{B1} .

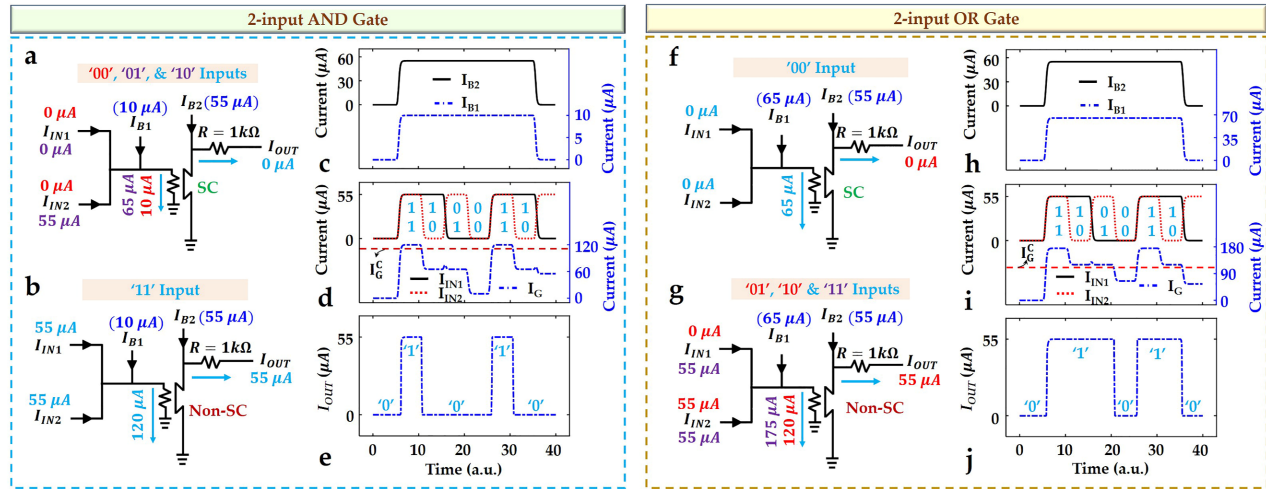


FIG. 4. 2-Input AND and OR operations. AND operation with the proposed reconfigurable circuit for (a) 00, 01, and 10 and (b) 11 input combinations. (c)–(e) Simulated time dynamics for the AND operation. Illustration of the OR operation for (f) 00 and (g) 01, 10, and 11 input combinations. (h)–(j) Time dynamics of the OR operation where the channel switches for the 11 combination due to the choice of I_{B1} .

building a 1-bit full adder, the use of majority can reduce the logic level by 50% and 57.14% compared to the NAND and NOR implementations, respectively, and can also reduce the number of required cycles by 60%.²⁶

Here, we show that the same circuit with a single hTron device can be reconfigured to perform 3-input majority logic operation. Here, we use $I_{B1} = 10 \mu\text{A}$. As a result, when there is less number of logic 1 among the inputs, the gate terminal does not get sufficient current to switch the channel [Fig. 5(a)]. On the other hand, when there is more number of logic 1 inputs, the total gate current exceeds I_G^C , and the channel switches to its non-superconducting state [Fig. 5(b)]. As seen in the transient results of Figs. 5(c)–5(e), the same circuit can perform the 3-input majority logic function.

We demonstrate a single hTron-based reconfigurable logic circuit that can perform 1-input copy and NOT, 2-input AND and OR, and

3-input majority operations by only choosing suitable biasing conditions. Our proposed logic circuit benefits from useful features of the hTron, including low turn-on-time, input–output isolation, low power operation, and so on.¹² Moreover, hTron devices do not need any superconducting loop like other superconducting devices such as JJs and SQUIDs. Therefore, our proposed logic circuit will not suffer from any flux trapping issue and will be able to solve the scalability issue of the JJ and SQUID-based circuits. Typically, the number of required devices in a logic gate increases with the number of inputs, which is not the case for our design. We use the same circuit based on one hTron device to reconfigurably perform all these basic operations, enabling the implementation of a superconducting processing unit with a much less number of devices compared with the existing approaches. Moreover, since we are using the same circuit for different logic operations, we can develop a camouflaged processing unit, where all the logic gates will have the same layout and will reduce the risk of reverse engineering.

Also, thanks to the high impedance ($\gg 1 \text{ k}\Omega$) non-superconducting state of hTron devices, the cascability of the proposed logic circuit is not a concern like the other current-controlled superconducting logic gates. One hTron can drive other resistive gate terminals (typically has an impedance of $1 \text{ k}\Omega$) of the next stage logic circuits. Additionally, our proposed copy gate can be used to develop a current splitter circuit like the one proposed in Ref. 27 to enable larger fanout.

Finally, hTron devices suffer from reset time limitations due to the thermal recovery after each switching and so will be the case for our proposed circuit. To solve this issue, a different superconductor with a suitable thickness (for example, NbN with $\sim 1 \text{ ns}$ thermal reset time²⁸) or the same superconductor with different thicknesses can be used to make the channel microwire. Furthermore, our proposed circuit is not limited to thermal hTron devices. Our proposal will be applicable to any device that shows gate-controlled switching between superconducting and non-superconducting states like Josephson junction FET,^{16,29} dayem transistor,^{30,31} ferroelectric SQUID,^{11,15} and so on.

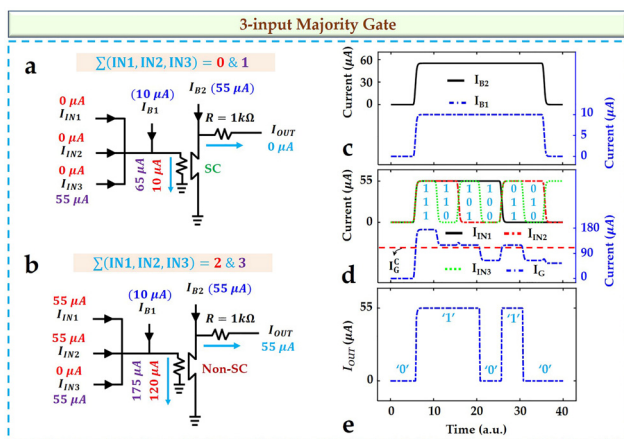


FIG. 5. 3-Input majority operation. Illustration of majority logic when there are (a) more and (b) less number of logic 1 inputs. (c)–(e) Simulated time dynamics of the majority operation.

See the supplementary material for the detailed discussion on fabrication and electrical characterization of the heater cryotron (hTron) device.

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AUTHOR DECLARATIONS

Conflict of Interest

The authors have no conflicts to disclose.

Author Contributions

Shamiul Alam: Conceptualization (equal); Formal analysis (equal); Methodology (equal); Visualization (equal); Writing – original draft (equal). **Dana Rampini:** Data curation (equal). **Bakhrom Oripov:** Data curation (equal). **Adam N. McCaughan:** Data curation (equal); Funding acquisition (equal); Project administration (equal); Writing – review & editing (equal). **Ahmedullah Aziz:** Funding acquisition (equal); Project administration (equal); Supervision (equal); Writing – review & editing (equal).

DATA AVAILABILITY

The data that support the plots within this paper and other findings of this study are available from the corresponding author upon reasonable request.

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